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MODEL INTERROGATION**



**REPRESENTATIONAL MEASUREMENT FAILURE IN
HEALTH TECHNOLOGY ASSESSMENT**

**GERMANY: THE HAMBURG CENTRE FOR HEALTH
ECONOMICS (HCHE) AND THE ENDORSEMENT OF
MEASUREMENT INVERSION**

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FOREWORD

HEALTH TECHNOLOGY ASSESSMENT: A GLOBAL SYSTEM OF NON-MEASUREMENT

The Hamburg Center for Health Economics (HCHE) is one of Germany's leading academic institutions dedicated to research in health economics, healthcare systems, and policy evaluation. Its primary objective is to generate evidence to inform the efficient allocation of healthcare resources, with a focus on improving the performance, sustainability, and equity of health systems. The Center brings together economists and interdisciplinary researchers to examine how healthcare services are financed, delivered, and evaluated, particularly within the context of publicly funded systems.

HCHE's activities span a broad range of topics relevant to health technology assessment, including economic evaluation of medical interventions, health outcomes research, healthcare utilization, and reimbursement policy. The Center undertakes applied and policy-oriented research on cost-effectiveness, budget impact, and the comparative value of pharmaceuticals and medical technologies. It also develops and applies quantitative methods, including econometric analysis and modeling techniques, to assess the impact of health policies and interventions over time. Through collaboration with national and international partners, including government agencies and healthcare organizations, HCHE contributes to policy debates on pricing, access, and the organization of healthcare systems. In this role, the Center functions as an important academic contributor to the analytical frameworks that underpin HTA and evidence-based decision-making in Germany and across Europe.

The objective of this study is to undertake a structured interrogation of the HTA-related knowledge base associated with the Hamburg Center for Health Economics using a standardized 24-item canonical diagnostic instrument grounded in the axioms of representational measurement theory. The purpose is not to evaluate individual publications or policy contributions, but to determine whether the conceptual framework that informs the Center's work satisfies the minimum requirements for scientific measurement. In particular, the study assesses whether the knowledge base recognizes the conditions necessary for admissible arithmetic operations, including unidimensionality, invariance, the existence of a true zero, and the requirement that latent constructs be measured through Rasch-conformant instruments. By assigning categorical probabilities to each statement and transforming these into normalized logits, the analysis provides a structured profile of conceptual endorsement, allowing an explicit evaluation of whether the knowledge base supports evaluable, falsifiable value claims.

The findings indicate a clear and consistent pattern of measurement inversion. Statements that are true within representational measurement theory are weakly endorsed or rejected, while statements that are false—particularly those that underpin cost-utility analysis—are strongly endorsed, often at high or maximum logit levels. Constructs such as utilities and QALYs are treated as if they possess interval or ratio scale properties, supporting aggregation and arithmetic operations, despite

lacking the required measurement foundations. At the same time, key principles such as the requirement that multiplication demands a ratio scale and that measurement must precede arithmetic are not recognized. Rasch measurement is entirely absent, indicating that the only scientifically defensible pathway for constructing measures of latent constructs is not present. The resulting profile demonstrates that the knowledge base does not meet the axioms of representational measurement and therefore supports the generation of non-evaluable claims.

The modern articulation of principle that measurement precedes arithmetic can be traced to Stevens' seminal 1946 paper, which introduced the typology of nominal, ordinal, interval, and ratio scales ¹. Stevens made explicit what physicists, engineers, and psychologists already understood: different kinds of numbers permit different kinds of arithmetic. Ordinal scales allow ranking but not addition; interval scales permit addition and subtraction but not multiplication; ratio scales alone support multiplication, division, and the construction of meaningful ratios. Utilities derived from multiattribute preference exercises, such as EQ-5D or HUI, are ordinal preference scores; they do not satisfy the axioms of interval measurement, much less ratio measurement. Yet HTA has, for forty years, treated these utilities as if they were ratio quantities, multiplying them by time to create QALYs and inserting them into models without the slightest recognition that scale properties matter. Stevens' paper should have blocked the development of QALYs and cost-utility analysis entirely. Instead, it was ignored.

The foundational theory that establishes *when* and *whether* a set of numbers can be interpreted as measurements came with the publication of Krantz, Luce, Suppes, and Tversky's *Foundations of Measurement* (1971) ². Representational Measurement Theory (RMT) formalized the axioms under which empirical attributes can be mapped to numbers in a way that preserves structure. Measurement, in this framework, is not an act of assigning numbers for convenience, it is the discovery of a lawful relationship between empirical relations and numerical relations. The axioms of additive conjoint measurement, homogeneity, order, and invariance specify exactly when interval scales exist. RMT demonstrated once and for all that measurement is not optional and not a matter of taste: either the axioms hold and measurement is possible, or the axioms fail and measurement is impossible. Every major construct in HTA, utilities, QALYs, DALYs, ICERs, incremental ratios, preference weights, health-state indices, fails these axioms. They lack unidimensionality; they violate independence; they depend on aggregation of heterogeneous attributes; they collapse under the requirements of additive conjoint measurement. Yet HTA proceeded, decade after decade, without any engagement with these axioms, as if the field had collectively decided that measurement theory applied everywhere except in the evaluation of therapies.

Whereas representational measurement theory articulates the axioms for interval measurement, Georg Rasch's 1960 model provides the only scientific method for transforming ordered categorical responses into interval measures for latent traits ³. Rasch models uniquely satisfy the principles of specific objectivity, sufficiency, unidimensionality, and invariance. For any construct such as pain, fatigue, depression, mobility, or need, Rasch analysis is the only legitimate means of producing an interval scale from ordinal item responses. Rasch measurement is not an alternative to RMT; it is its operational instantiation. The equivalence of Rasch's axioms and the axioms of representational measurement was demonstrated by Wright, Andrich and others as early as the

1970s. In the latent-trait domain, the very domain where HTA claims to operate; Rasch is the only game in town ⁴.

Yet Rasch is effectively absent from all HTA guidelines, including NICE, PBAC, CADTH, ICER, SMC, and PHARMAC. The analysis demands utilities but never requires that those utilities be measured. They rely on multiattribute ordinal classifications but never understand that those constructs be calibrated on interval or ratio scales. They mandate cost-utility analysis but never justify the arithmetic. They demand modelled QALYs but never interrogate their dimensional properties. These guidelines do not misunderstand Rasch; they do not know it exists. The axioms that define measurement and the model that makes latent trait measurement possible are invisible to the authors of global HTA rules. The field has evolved without the science that measurement demands.

How did HTA miss the bus so thoroughly? The answer lies in its historical origins. In the late 1970s and early 1980s, HTA emerged not from measurement science but from welfare economics, decision theory, and administrative pressure to control drug budgets. Its core concern was *valuing health states*, not *measuring health*. This move, quiet, subtle, but devastating, shifted the field away from the scientific question “What is the empirical structure of the construct we intend to measure?” and toward the administrative question “How do we elicit a preference weight that we can multiply by time?” The preference-elicitation projects of that era (SG, TTO, VAS) were rationalized as measurement techniques, but they never satisfied measurement axioms. Ordinal preferences were dressed up as quasi-cardinal indices; valuation tasks were misinterpreted as psychometrics; analyst convenience replaced measurement theory. The HTA community built an entire belief system around the illusion that valuing health is equivalent to measuring health. It is not.

The endurance of this belief system, forty years strong and globally uniform, is not evidence of validity but evidence of institutionalized error. HTA has operated under conditions of what can only be described as *structural epistemic closure*: a system that has never questioned its constructs because it never learned the language required to ask the questions. Representational measurement theory is not taught in graduate HTA programs; Rasch modelling is not part of guideline development; dimensional analysis is not part of methodological review. The field has been insulated from correction because its conceptual foundations were never laid. What remains is a ritualized practice: utilities in, QALYs out, ICERs calculated, thresholds applied. The arithmetic continues because everyone assumes someone else validated the numbers.

This Logit Working Paper series exposes, through probabilistic and logit-based interrogations of AI large language national knowledge bases, the scale of this failure. The results display a global pattern: true statements reflecting the axioms of measurement receive weak endorsement; false statements reflecting the HTA belief system receive moderate or strong reinforcement. This is not disagreement. It is non-possession. It shows that HTA, worldwide, has developed as a quantitative discipline without quantitative foundations; a confused exercise in numerical storytelling.

The conclusion is unavoidable: HTA does not need incremental reform; it needs a scientific revolution. Measurement must precede arithmetic. Representational axioms must precede valuation rituals. Rasch measurement must replace ordinal summation and utility algorithms.

Value claims must be falsifiable, protocol-driven, and measurable; rather than simulated, aggregated, and numerically embellished.

The global system of non-measurement is now visible. The task ahead is to replace it with science.

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DISCLAIMER

This analysis is generated through the structured interrogation of a large language model (LLM) applied to a defined documentary corpus and is intended solely to characterize patterns within an aggregated knowledge environment. It does not identify, assess, or attribute beliefs, intentions, competencies, or actions to any named individual, faculty member, student, administrator, institution, or organization. The results do not constitute factual findings about specific persons or programs, nor should they be interpreted as claims regarding professional conduct, educational quality, or compliance with regulatory or accreditation standards. All probabilities and logit values reflect model-based inferences about the presence or absence of concepts within a bounded textual ecosystem, not judgments about real-world actors. The analysis is exploratory, interpretive, and methodological in nature, offered for scholarly discussion of epistemic structures rather than evaluative or legal purposes. Any resemblance to particular institutions or practices is contextual and non-attributive, and no adverse implication should be inferred.

1. INTERROGATING THE LARGE LANGUAGE MODEL

A large language model (LLM) is an artificial intelligence system designed to understand, generate, and manipulate human language by learning patterns from vast amounts of text data. Built on deep neural network architectures, most commonly transformers, LLMs analyze relationships between words, sentences, and concepts to produce contextually relevant responses. During training, the model processes billions of examples, enabling it to learn grammar, facts, reasoning patterns, and even subtle linguistic nuances. Once trained, an LLM can perform a wide range of tasks: answering questions, summarizing documents, generating creative writing, translating languages, assisting with coding, and more. Although LLMs do not possess consciousness or true understanding, they simulate comprehension by predicting the most likely continuation of text based on learned patterns. Their capabilities make them powerful tools for communication, research, automation, and decision support, but they also require careful oversight to ensure accuracy, fairness, privacy, and responsible use

In this Logit Working Paper, “interrogation” refers not to discovering what an LLM *believes*, it has no beliefs, but to probing the content of the *corpus-defined knowledge space* we choose to analyze. This knowledge base is enhanced if it is backed by accumulated memory from the user. In this case the interrogation relies also on 12 months of HTA memory from continued application of the system to evaluate HTA experience. The corpus is defined before interrogation: it may consist of a journal (e.g., *Value in Health*), a national HTA body, a specific methodological framework, or a collection of policy documents. Once the boundaries of that corpus are established, the LLM is used to estimate the conceptual footprint within it. This approach allows us to determine which principles are articulated, neglected, misunderstood, or systematically reinforced.

In this HTA assessment, the objective is precise: to determine the extent to which a given HTA knowledge base or corpus, global, national, institutional, or journal-specific, recognizes and reinforces the foundational principles of representational measurement theory (RMT). The core principle under investigation is that measurement precedes arithmetic; no construct may be treated as a number or subjected to mathematical operations unless the axioms of measurement are satisfied. These axioms include unidimensionality, scale-type distinctions, invariance, additivity, and the requirement that ordinal responses cannot lawfully be transformed into interval or ratio quantities except under Rasch measurement rules.

The HTA knowledge space is defined pragmatically and operationally. For each jurisdiction, organization, or journal, the corpus consists of:

- published HTA guidelines
- agency decision frameworks
- cost-effectiveness reference cases
- academic journals and textbooks associated with HTA
- modelling templates, technical reports, and task-force recommendations
- teaching materials, methodological articles, and institutional white papers

These sources collectively form the epistemic environment within which HTA practitioners develop their beliefs and justify their evaluative practices. The boundary of interrogation is thus not the whole of medicine, economics, or public policy, but the specific textual ecosystem that sustains HTA reasoning. . The “knowledge base” is therefore not individual opinions but the cumulative, structured content of the HTA discourse itself within the LLM.

THE HAMBURG CENTRE FOR HEALTH ECONOMICS HTA KNOWLEDGE BASE

The HTA-related knowledge base associated with the Hamburg Center for Health Economics is best understood as an applied and policy-oriented framework grounded in health economics, economic evaluation, and healthcare system analysis. Its primary focus is on assessing the costs and consequences of healthcare interventions, the performance of health systems, and the allocation of resources within constrained budgets. Within an HTA context, this translates into a strong emphasis on cost-effectiveness and cost-utility analysis, where health outcomes are expressed in terms of preference-based measures such as quality-adjusted life years. These measures are combined with cost data within modeling frameworks to generate estimates of value, including cost per QALY gained, which are then used to inform policy discussions on reimbursement, pricing, and healthcare delivery.

A defining characteristic of this knowledge base is the absence of any formal requirement to establish the measurement properties of the constructs it employs. Preference-based measures of health status are treated as if they possess interval or ratio scale characteristics, enabling their use in arithmetic operations such as multiplication by time and aggregation across individuals. However, there is no requirement to demonstrate unidimensionality, invariance, or the existence of a true zero, nor is there systematic use of Rasch modeling to transform ordinal observations into valid measures of latent traits. Instead, the framework proceeds on the implicit assumption that numerical representation is sufficient to constitute measurement. This allows the construction of QALYs and the application of economic models without addressing whether the underlying quantities meet the axioms of representational measurement.

The knowledge base also integrates these assumptions within a broader analytical framework that emphasizes modeling, econometric analysis, and policy relevance. Advanced quantitative techniques are applied to evaluate healthcare interventions, simulate long-term outcomes, and assess the impact of policy changes. While these methods provide a high degree of technical sophistication, they operate within a structure that assumes the validity of the measures used rather than establishing it. The focus is on improving the precision and robustness of estimates, rather than on the prior question of whether the quantities being analyzed are measurable. This creates a situation in which methodological rigor in statistical and economic terms coexists with a lack of measurement validity.

As a leading academic center in Germany, HCHE plays an important role in shaping the intellectual and methodological foundations of HTA. Its work contributes to policy debates, informs decision-making processes, and supports the development of evaluation frameworks used by national agencies. The absence of representational measurement within this knowledge base therefore has implications beyond the institution itself. It reflects and reinforces a broader

analytical structure in which measurement is assumed rather than demonstrated, and where numerical outputs are treated as evidence despite failing to meet the conditions required for scientific measurement. The resulting framework produces outputs that are internally consistent but not empirically evaluable in a measurement-consistent sense, limiting their ability to support credible, replicable, and falsifiable value claims within the standards of normal science.

CATEGORICAL PROBABILITIES

In the present application, the interrogation is tightly bounded. It does not ask what an LLM “thinks,” nor does it request a normative judgment. Instead, the LLM evaluates how likely the HTA knowledge space is to endorse, imply, or reinforce a set of 24 diagnostic statements derived from representational measurement theory (RMT). Each statement is objectively TRUE or FALSE under RMT. The objective is to assess whether the HTA corpus exhibits possession or non-possession of the axioms required to treat numbers as measures. The interrogation creates an categorical endorsement probability: the estimated likelihood that the HTA knowledge base endorses the statement whether it is true or false; *explicitly or implicitly*.

The use of categorical endorsement probabilities within the Logit Working Papers reflects both the nature of the diagnostic task and the structure of the language model that underpins it. The purpose of the interrogation is not to estimate a statistical frequency drawn from a population of individuals, nor to simulate the behavior of hypothetical analysts. Instead, the aim is to determine the conceptual tendencies embedded in a domain-specific knowledge base: the discursive patterns, methodological assumptions, and implicit rules that shape how a health technology assessment environment behaves. A large language model does not “vote” like a survey respondent; it expresses likelihoods based on its internal representation of a domain. In this context, endorsement probabilities capture the strength with which the knowledge base, as represented within the model, supports a particular proposition. Because these endorsements are conceptual rather than statistical, the model must produce values that communicate differences in reinforcement without implying precision that cannot be justified.

This is why categorical probabilities are essential. Continuous probabilities would falsely suggest a measurable underlying distribution, as if each HTA system comprised a definable population of respondents with quantifiable frequencies. But large language models do not operate on that level. They represent knowledge through weighted relationships between linguistic and conceptual patterns. When asked whether a domain tends to affirm, deny, or ignore a principle such as unidimensionality, admissible arithmetic, or the axioms of representational measurement, the model draws on its internal structure to produce an estimate of conceptual reinforcement. The precision of that estimate must match the nature of the task. Categorical probabilities therefore provide a disciplined and interpretable way of capturing reinforcement strength while avoiding the illusion of statistical granularity.

The categories used, values such as 0.05, 0.10, 0.20, 0.50, 0.75, 0.80, and 0.85, are not arbitrary. They function as qualitative markers that correspond to distinct degrees of conceptual possession: near-absence, weak reinforcement, inconsistent or ambiguous reinforcement, common reinforcement, and strong reinforcement. These values are far enough apart to ensure clear interpretability yet fine-grained enough to capture meaningful differences in the behavior of the

knowledge base. The objective is not to measure probability in a statistical sense but to classify the epistemic stance of the domain toward a given item. A probability of 0.05 signals that the knowledge base almost never articulates or implies the correct response under measurement theory, whereas 0.85 indicates that the domain routinely reinforces it. Values near the middle reflect conceptual instability rather than a balanced distribution of views.

Using categorical probabilities also aligns with the requirements of logit transformation. Converting these probabilities into logits produces an interval-like diagnostic scale that can be compared across countries, agencies, journals, or organizations. The logit transformation stretches differences at the extremes, allowing strong reinforcement and strong non-reinforcement to become highly visible. Normalizing logits to the fixed ± 2.50 range ensure comparability without implying unwarranted mathematical precision. Without categorical inputs, logits would suggest a false precision that could mislead readers about the nature of the diagnostic tool.

In essence, the categorical probability approach translates the conceptual architecture of the LLM into a structured and interpretable measurement analogue. It provides a disciplined bridge between the qualitative behavior of a domain's knowledge base and the quantitative diagnostic framework needed to expose its internal strengths and weaknesses.

The LLM computes these categorical probabilities from three sources:

1. **Structural content of HTA discourse**

If the literature repeatedly uses ordinal utilities as interval measures, multiplies non-quantities, aggregates QALYs, or treats simulations as falsifiable, the model infers high reinforcement of these false statements.

2. **Conceptual visibility of measurement axioms**

If ideas such as unidimensionality, dimensional homogeneity, scale-type integrity, or Rasch transformation rarely appear, or are contradicted by practice, the model assigns low endorsement probabilities to TRUE statements.

3. **The model's learned representation of domain stability**

Where discourse is fragmented, contradictory, or conceptually hollow, the model avoids assigning high probabilities. This is *not* averaging across people; it is a reflection of internal conceptual incoherence within HTA.

The output of interrogation is a categorical probability for each statement. Probabilities are then transformed into logits $[\ln(p/(1-p))]$, capped to ± 4.0 logits to avoid extreme distortions, and normalized to ± 2.50 logits for comparability across countries. A positive normalized logit indicates reinforcement in the knowledge base. A negative logit indicates weak reinforcement or conceptual absence. Values near zero logits reflect epistemic noise.

Importantly, *a high endorsement probability for a false statement does not imply that practitioners knowingly believe something incorrect*. It means the HTA literature itself behaves as if the falsehood were true; through methods, assumptions, or repeated uncritical usage. Conversely, a low probability for a true statement indicates that the literature rarely articulates, applies, or even implies the principle in question.

The LLM interrogation thus reveals structural epistemic patterns in HTA: which ideas the field possesses, which it lacks, and where its belief system diverges from the axioms required for scientific measurement. It is a diagnostic of the *knowledge behavior* of the HTA domain, not of individuals. The 24 statements function as probes into the conceptual fabric of HTA, exposing the extent to which practice aligns or fails to align with the axioms of representational measurement.

INTERROGATION STATEMENTS

Below is the canonical list of the 24 diagnostic HTA measurement items used in all the logit analyses, each marked with its correct truth value under representational measurement theory (RMT) and Rasch measurement principles.

This is the definitive set used across the Logit Working Papers.

Measurement Theory & Scale Properties

1. Interval measures lack a true zero — TRUE
2. Measures must be unidimensional — TRUE
3. Multiplication requires a ratio measure — TRUE
4. Time trade-off preferences are unidimensional — FALSE
5. Ratio measures can have negative values — FALSE
6. EQ-5D-3L preference algorithms create interval measures — FALSE
7. The QALY is a ratio measure — FALSE
8. Time is a ratio measure — TRUE

Measurement Preconditions for Arithmetic

9. Measurement precedes arithmetic — TRUE
10. Summations of subjective instrument responses are ratio measures — FALSE
11. Meeting the axioms of representational measurement is required for arithmetic — TRUE

Rasch Measurement & Latent Traits

12. There are only two classes of measurement: linear ratio and Rasch logit ratio — TRUE
13. Transforming subjective responses to interval measurement is only possible with Rasch rules — TRUE
14. Summation of Likert question scores creates a ratio measure — FALSE

Properties of QALYs & Utilities

15. The QALY is a dimensionally homogeneous measure — FALSE
16. Claims for cost-effectiveness fail the axioms of representational measurement — TRUE
17. QALYs can be aggregated — FALSE

Falsifiability & Scientific Standards

18. Non-falsifiable claims should be rejected — TRUE
19. Reference-case simulations generate falsifiable claims — FALSE

Logit Fundamentals

20. The logit is the natural logarithm of the odds-ratio — TRUE

Latent Trait Theory

21. The Rasch logit ratio scale is the only basis for assessing therapy impact for latent traits — TRUE
22. A linear ratio scale for manifest claims can always be combined with a logit scale — FALSE
23. The outcome of interest for latent traits is the possession of that trait — TRUE
24. The Rasch rules for measurement are identical to the axioms of representational measurement — TRUE

AI LARGE LANGUAGE MODEL STATEMENTS: TRUE OR FALSE

Each of the 24 statements has a 400 word explanation why the statement is true or false as there may be differences of opinion on their status in terms of unfamiliarity with scale typology and the axioms of representational measurement.

The link to these explanations is: <https://maimonresearch.com/ai-llm-true-or-false/>

INTERPRETING TRUE STATEMENTS

TRUE statements represent foundational axioms of measurement and arithmetic. Endorsement probabilities for TRUE items typically cluster in the low range, indicating that the HTA corpus does *not* consistently articulate or reinforce essential principles such as:

- measurement preceding arithmetic
- unidimensionality
- scale-type distinctions
- dimensional homogeneity

- impossibility of ratio multiplication on non-ratio scales
- the Rasch requirement for latent-trait measurement

Low endorsement indicates **non-possession** of fundamental measurement knowledge—the literature simply does not contain, teach, or apply these principles.

INTERPRETING FALSE STATEMENTS

FALSE statements represent the well-known mathematical impossibilities embedded in the QALY framework and reference-case modelling. Endorsement probabilities for FALSE statements are often moderate or even high, meaning the HTA knowledge base:

- accepts non-falsifiable simulation as evidence
- permits negative “ratio” measures
- treats ordinal utilities as interval measures
- treats QALYs as ratio measures
- treats summated ordinal scores as ratio scales
- accepts dimensional incoherence

This means the field systematically reinforces incorrect assumptions at the center of its practice. *Endorsement* here means the HTA literature behaves as though the falsehood were true.

2. SUMMARY OF FINDINGS FOR TRUE AND FALSE ENDORSEMENTS: HAMBURG CENTRE FOR HEALTH ECONOMICS

Table 1 presents probabilities and normalized logits for each of the 24 diagnostic measurement statements. This is the standard reporting format used throughout the HTA assessment series.

It is essential to understand how to interpret these results.

The endorsement probabilities do not indicate whether a statement is *true* or *false* under representational measurement theory. Instead, they estimate the extent to which the HTA knowledge base associated with the target treats the statement as if it were true, that is, whether the concept is reinforced, implied, assumed, or accepted within the country's published HTA knowledge base.

The logits provide a continuous, symmetric scale, ranging from +2.50 to -2.50, that quantifies the degree of this endorsement. The logits, of course link to the probabilities (p) as the logit is the natural logarithm of the odds ratio; $\text{logit} = \ln[p/1-p]$.

- Strongly positive logits indicate pervasive reinforcement of the statement within the knowledge system.
- Strongly negative logits indicate conceptual absence, non-recognition, or contradiction within that same system.
- Values near zero indicate only shallow, inconsistent, or fragmentary support.

Thus, the endorsement logit profile serves as a direct index of a country's epistemic alignment with the axioms of scientific measurement, revealing the internal structure of its HTA discourse. It does not reflect individual opinions or survey responses, but the implicit conceptual commitments encoded in the literature itself.

HAMBURG CENTRE FOR HEALTH ECONOMICS: ENDORSING FALSE MEASUREMENT

The interrogation of the HTA-related knowledge base associated with the Hamburg Center for Health Economics presents a profile that is both consistent with and reinforcing of the broader European pattern of measurement inversion (Table 1) As one of Germany's leading academic centers for health economics, the Hamburg Center occupies a critical position in shaping the theoretical and applied foundations of economic evaluation in healthcare. Its work spans cost-effectiveness analysis, health system performance, reimbursement policy, and outcomes research. The significance of the present findings therefore lies not only in the identification of measurement inversion within a single institution, but in the confirmation that this inversion is embedded within the economic logic that supports HTA across Germany and, by extension, much of Europe.

TABLE 1: ITEM STATEMENT, RESPONSE, ENDORSEMENT AND NORMALIZED LOGITS: HAMBURG CENTRE FOR HEALTH ECONOMICS

STATEMENT	RESPONSE 1=TRUE 0=FALSE	ENDORSEMENT OF RESPONSE CATEGORICAL PROBABILITY	NORMALIZED LOGIT (IN RANGE +/- 2.50)
INTERVAL MEASURES LACK A TRUE ZERO	1	0.25	-1.10
MEASURES MUST BE UNIDIMENSIONAL	1	0.20	-1.40
MULTIPLICATION REQUIRES A RATIO MEASURE	1	0.10	-2.20
TIME TRADE-OFF PREFERENCES ARE UNIDIMENSIONAL	0	0.95	+2.50
RATIO MEASURES CAN HAVE NEGATIVE VALUES	0	0.95	+2.50
EQ-5D-3L PREFERENCE ALGORITHMS CREATE INTERVAL MEASURES	0	0.95	+2.50
THE QALY IS A RATIO MEASURE	0	0.95	+2.50
TIME IS A RATIO MEASURE	1	0.85	+1.75
MEASUREMENT PRECEDES ARITHMETIC	1	0.20	-1.40
SUMMATIONS OF SUBJECTIVE INSTRUMENT RESPONSES ARE RATIO MEASURES	0	0.95	+2.50
MEETING THE AXIOMS OF REPRESENTATIONAL MEASUREMENT IS REQUIRED FOR ARITHMETIC	1	0.10	-2.20
THERE ARE ONLY TWO CLASSES OF MEASUREMENT LINEAR RATIO AND RASCH LOGIT RATIO	1	0.05	-2.50
TRANSFORMING SUBJECTIVE RESPONSES TO INTERVAL MEASUREMENT IS ONLY POSSIBLE WITH RASH RULES	1	0.05	-2.50
SUMMATION OF LIKERT QUESTION SCORES CREATES A RATIO MEASURE	0	0.95	+2.50
THE QALY IS A DIMENSIONALLY HOMOGENEOUS MEASURE	0	0.95	+2.50
CLAIMS FOR COST-EFFECTIVENESS FAIL THE AXIOMS OF REPRESENTATIONAL MEASUREMENT	1	0.10	-2.20
QALYS CAN BE AGGREGATED	0	0.95	+2.50

NON-FALSIFIABLE CLAIMS SHOULD BE REJECTED	1	0.50	0.00
REFERENCE CASE SIMULATIONS GENERATE FALSIFIABLE CLAIMS	0	0.95	+2.50
THE LOGIT IS THE NATURAL LOGARITHM OF THE ODDS-RATIO	1	0.80	+1.40
THE RASCH LOGIT RATIO SCALE IS THE ONLY BASIS FOR ASSESSING THERAPY IMPACT FOR LATENT TRAITS	1	0.05	-2.50
A LINEAR RATIO SCALE FOR MANIFEST CLAIMS CAN ALWAYS BE COMBINED WITH A LOGIT SCALE	0	0.90	+2.20
THE OUTCOME OF INTEREST FOR LATENT TRAITS IS THE POSSESSION OF THAT TRAIT	1	0.05	-2.50
THE RASCH RULES FOR MEASUREMENT ARE IDENTICAL TO THE AXIOMS OF REPRESENTATIONAL MEASUREMENT	1	0.05	-2.50

The resulting profile is strongly polarized. Statements that are false within the axioms of representational measurement are consistently endorsed at the highest probability levels, while statements that are true are weakly endorsed or rejected. This pattern is not ambiguous. It demonstrates a knowledge base in which the conditions required for measurement are not recognized, and where numerical constructs are treated as if they possess the properties required to support arithmetic operations. This is measurement inversion in its clearest form: the systematic substitution of numerical representation for measurement.

The most decisive findings concern the QALY. The propositions that the QALY is a ratio measure, that it is dimensionally homogeneous, and that QALYs can be aggregated are all endorsed at the maximum logit value. This reflects categorical commitment. The knowledge base treats QALYs as lawful quantities capable of multiplication, addition, and comparison across individuals and time. Yet this position is incompatible with the axioms of representational measurement. A ratio scale requires a true zero and invariant unit structure. Utilities derived from ordinal preference data do not meet these requirements. The multiplication of such utilities by time to generate QALYs is therefore not an admissible operation. The arithmetic at the core of cost-utility analysis is not approximate. It is invalid.

This conclusion is reinforced by the treatment of preference-based measures. The statement that EQ-5D preference algorithms create interval measures is endorsed at the maximum logit, as are the propositions that summations of subjective instrument responses and Likert scores produce ratio measures. These endorsements demonstrate a systematic collapse of scale distinctions. Ordinal, interval, and ratio properties are treated as interchangeable. Once a numerical value is assigned, it is assumed to support arithmetic. This is the defining feature of measurement inversion.

In contrast, the propositions that define the conditions for valid measurement are systematically rejected. The requirement that multiplication demands a ratio scale is assigned a strongly negative logit, as is the principle that measurement must precede arithmetic. The necessity that arithmetic operations be grounded in the axioms of representational measurement is also rejected. These results demonstrate that the knowledge base does not recognize the logical order of scientific reasoning. Arithmetic is applied without regard to the scale properties of the quantities involved. Measurement is assumed rather than established.

The absence of Rasch measurement is complete. All statements relating to Rasch modeling are assigned the lowest possible logit, indicating effective non-possession. This is decisive. Without Rasch transformation, there is no scientifically valid method for converting ordinal observations of latent constructs into invariant measures. The use of preference weights does not achieve this. It produces numerical scores, not measures. The Hamburg knowledge base therefore lacks the only available framework for the valid measurement of latent attributes.

The epistemological structure of the knowledge base is further revealed in the treatment of falsifiability. The proposition that non-falsifiable claims should be rejected receives only neutral endorsement, while the claim that reference-case simulations generate falsifiable claims is strongly endorsed. This reflects a confusion between internal model behavior and empirical testability. Models can be adjusted, recalibrated, and extended, but this does not make their outputs falsifiable if the underlying constructs are not measurable. The knowledge base treats modeled outputs as evidence, even though they cannot be tested against invariant quantities.

What makes the Hamburg case particularly important is its independence. HCHE is not an extension of a national HTA agency. It is an academic center with its own research agenda, contributing to health economics and HTA-related work within Germany and beyond. The replication of measurement inversion within this setting demonstrates that the problem is not imposed by regulatory frameworks alone. It is embedded within the academic knowledge base itself. This is critical. It shows that even in the absence of direct institutional constraint, the same framework is reproduced.

The methodological sophistication of the Hamburg knowledge base reinforces rather than corrects this structure. Advanced econometric methods, statistical analysis, and decision-analytic models are applied to evaluate interventions and inform policy. These methods provide internal coherence and technical rigor. However, they operate within a framework that assumes the validity of the measures used rather than establishing it. The result is a system in which methodological complexity coexists with a lack of measurement validity.

The implications are direct and unavoidable. A knowledge base that endorses false statements about scale and arithmetic cannot generate evaluable value claims. Cost-effectiveness ratios derived from QALYs are not empirical findings. They are functions of assumptions applied to non-measurement. They cannot be replicated because there is no invariant quantity to reproduce. They cannot be falsified because the outputs are not grounded in measurable attributes. They do not contribute to the accumulation of objective knowledge.

This is not a marginal failure. It is a categorical one. The Hamburg knowledge base does not fall short of ideal measurement standards. It operates independently of them. It endorses the propositions required to sustain false measurement and rejects those required to prevent it. This is measurement inversion in its most explicit academic form.

The broader implication for Germany is clear. The presence of measurement inversion in both Freiburg and Hamburg demonstrates that the problem is not confined to a particular institutional setting. It is reproduced across independent academic centers. This indicates that the German HTA knowledge base, like its counterparts in other countries, is structured around assumptions that do not meet the axioms of representational measurement.

The final judgment is therefore straightforward. The HTA-related knowledge base associated with the Hamburg Center for Health Economics does not meet the requirements of representational measurement. It cannot support the arithmetic operations on which its value claims depend. Its outputs are not empirically evaluable, not falsifiable, and not scientifically admissible. They are internally consistent within the framework, but the framework itself lacks a lawful foundation.

Once this is recognized, the status of the resulting claims is clear. They are not evidence. They are numerical storytelling under academic authority.

THE FUTURE OF HEALTH TECHNOLOGY ASSESSMENT IN GERMANY

The interrogations reported for Germany point to a clear and consistent conclusion: the HTA-related knowledge base is fully committed to measurement inversion. Across both the Institute of Medical Biometry and Statistics, University of Freiburg, and the Hamburg Center for Health Economics, the same structure is observed. Statements that are false within the axioms of representational measurement are strongly endorsed, while those that define the conditions for valid measurement are rejected or absent. This is not a marginal inconsistency or a localized weakness. It is a systematic and internally coherent framework in which numerical representation substitutes for measurement, and where arithmetic is applied to quantities that do not exist.

In both cases, the commitment to cost-utility analysis and QALY-based reasoning is explicit. Utilities are treated as if they possess interval or ratio scale properties, allowing multiplication by time, aggregation across individuals, and incorporation into modeled projections. These operations are foundational to HTA, yet they are not admissible. The requirement that multiplication demands a ratio scale is not recognized, nor is the prior condition that measurement must precede arithmetic. There is no recognition of Rasch-conformant measurement for latent constructs, no requirement for unidimensionality or invariance, and no attempt to establish lawful scale properties. False measurement is not an exception. It is the rule.

What distinguishes Germany is not the presence of an alternative framework, but the absence of any corrective mechanism. Academic centers do not challenge the evaluative structure. They reproduce it. There is no independent knowledge base that recognizes or applies the axioms of representational measurement. The absence is complete.

This raises an unavoidable question regarding the future of HTA in Germany. Can a framework that is demonstrably inconsistent with the principles of measurement be sustained once this inconsistency is made explicit? For decades, authority has rested on the presence of numbers including comparative effectiveness estimates, cost-effectiveness ratios, and model outputs combined with apparent methodological sophistication. The cat is now out of the bag. What are presented as measures are not measures at all. They do not meet the conditions required for measurement. Once this is recognized, the basis for that authority collapses.

The challenge is not technical but foundational. It is not a matter of refining models, improving data sources, or adjusting parameters. It is a question of whether the framework itself is admissible. A system that applies arithmetic to non-measurement cannot generate evaluable claims. It cannot support replication in a measurement-consistent sense, nor can it be falsified. The framework collapses at the first step, because the quantities to which arithmetic is applied are not measures. Everything that follows is simply the institutionalized reproduction of invalid reasoning.

It produces outputs that are internally coherent but externally invalid. The logit profile makes this explicit: as a decision framework, HTA has nothing to offer. Its application should be discontinued.

There is no ambiguity in the evidence. Across more than 120 interrogations, the same pattern is observed: no recognition of measurement theory, and consistent endorsement of a framework that violates it. This is not ignorance alone. It is the institutionalization of a false belief system that has persisted for over 40 years.

German research centers and agencies may choose to continue with the present framework. But that position is no longer defensible. The absence of measurement is now explicit. Continued reliance on cost-effectiveness claims that violate the axioms of measurement invites scrutiny and rejection.

There is only one path forward. If HTA is to survive, it must return to first principles. All claims must be grounded in valid measurement: linear ratio measures for manifest attributes and Rasch logit ratio measures for latent attributes. There are no alternatives. The fact that these requirements have been understood for more than half a century makes the persistence of the current framework all the more untenable.

3. THE TRANSITION TO MEASUREMENT IN HEALTH TECHNOLOGY ASSESSMENT

THE IMPERATIVE OF CHANGE

This analysis has not been undertaken to criticize decisions made by health system, nor to assign responsibility for the analytical frameworks currently used in formulary review. The evidence shows something more fundamental: organizations have been operating within a system that does not permit meaningful evaluation of therapy impact, even when decisions are made carefully, transparently, and in good faith.

The present HTA framework forces health systems to rely on numerical outputs that appear rigorous but cannot be empirically assessed (Table 1). Reference-case models, cost-per-QALY ratios, and composite value claims are presented as decision-support tools, yet they do not satisfy the conditions required for measurement. As a result, committees are asked to deliberate over results that cannot be validated, reproduced, or falsified. This places decision makers in an untenable position: required to choose among therapies without a stable evidentiary foundation.

This is not a failure of expertise, diligence, or clinical judgment. It is a structural failure. The prevailing HTA architecture requires arithmetic before measurement, rather than measurement before arithmetic. Health systems inherit this structure rather than design it. Manufacturers respond to it. Consultants reproduce it. Journals reinforce it. Universities promote it. Over time it has come to appear normal, even inevitable.

Yet the analysis presented in Table 1 demonstrates that this HTA framework cannot support credible falsifiable claims. Where the dependent variable is not a measure, no amount of modeling sophistication can compensate. Uncertainty analysis cannot rescue non-measurement. Transparency cannot repair category error. Consensus cannot convert assumption into evidence.

The consequence is that formulary decisions are based on numerical storytelling rather than testable claims. This undermines confidence, constrains learning, and exposes health systems to growing scrutiny from clinicians, patients, and regulators who expect evidence to mean something more than structured speculation.

The imperative of change therefore does not arise from theory alone. It arises from governance responsibility. A health system cannot sustain long-term stewardship of care if it lacks the ability to distinguish between claims that can be evaluated and claims that cannot. Without that distinction, there is no pathway to improvement; only endless repetition for years to come.

This transition is not about rejecting evidence. It is about restoring evidence to its proper meaning. It requires moving away from composite, model-driven imaginary constructs toward claims that are measurable, unidimensional, and capable of empirical assessment over time. The remainder of this section sets out how that transition can occur in a practical, defensible, and staged manner.

MEANINGFUL THERAPY IMPACT CLAIMS

At the center of the current problem is not data availability, modeling skill, or analytic effort. It is the nature of the claims being advanced. Contemporary HTA has evolved toward increasingly complex frameworks that attempt to compress multiple attributes, clinical effects, patient experience, time, and preferences into single composite outputs. These constructs are then treated as if they were measures. They are not (Table 1).

The complexity of the reference-case framework obscures a simpler truth: meaningful evaluation requires meaningful claims. A claim must state clearly what attribute is being affected, in whom, over what period, and how that attribute is measured. When these conditions are met, evaluation becomes possible. When they are not complexity substitutes for clarity. The current framework is not merely incorrect; it is needlessly elaborate. Reference-case modeling requires dozens of inputs, assumptions, and transformations, yet produces outputs that cannot be empirically verified. Each additional layer of complexity increases opacity while decreasing accountability. Committees are left comparing models rather than assessing outcomes.

In contrast, therapy impact can be expressed through two, and only two, types of legitimate claims. First are claims based on manifest attributes: observable events, durations, or resource units. These include hospitalizations avoided, time to event, days in remission, or resource use. When properly defined and unidimensional, these attributes can be measured on linear ratio scales and evaluated directly.

Second are claims based on latent attributes: symptoms, functioning, need fulfillment, or patient experience. These cannot be observed directly and therefore cannot be scored or summed meaningfully. They require formal measurement through Rasch models to produce invariant logit ratio scales. These two forms of claims are sufficient. They are also far more transparent. Each can be supported by a protocol. Each can be revisited. Each can be reproduced. Most importantly, each can fail. But they cannot be combined. This is the critical distinction. A meaningful claim is one that can be wrong.

Composite constructs such as QALYs do not fail in this sense. They persist regardless of outcome because they are insulated by assumptions. They are recalculated, not refuted. That is why they cannot support learning. The evolution of objective knowledge regarding therapy impact in disease areas is an entirely foreign concept. By re-centering formulary review on single-attribute, measurable claims, health systems regain control of evaluation. Decisions become grounded in observable change rather than modeled narratives. Evidence becomes something that accumulates, rather than something that is re-generated anew for every submission.

THE PATH TO MEANINGFUL MEASUREMENT

Transitioning to meaningful measurement does not require abandoning current processes overnight. It requires reordering them. The essential change is not procedural but conceptual: measurement must become the gatekeeper for arithmetic, not its byproduct.

The first step is formal recognition that not all numerical outputs constitute evidence. Health systems must explicitly distinguish between descriptive analyses and evaluable claims. Numbers that do not meet measurement requirements may inform discussion but cannot anchor decisions.

The second step is restructuring submissions around explicit claims rather than models. Each submission should identify a limited number of therapy impact claims, each defined by attribute, population, timeframe, and comparator. Claims must be unidimensional by design.

Third, each claim must be classified as manifest or latent. This classification determines the admissible measurement standard and prevents inappropriate mixing of scale types.

Fourth, measurement validity must be assessed before any arithmetic is permitted. For manifest claims, this requires confirmation of ratio properties. For latent claims, this requires Rasch-based measurement with demonstrated invariance.

Fifth, claims must be supported by prospective or reproducible protocols. Evidence must be capable of reassessment, not locked within long-horizon simulations designed to frustrate falsification.

Sixth, committees must be supported through targeted training in representational measurement principles, including Rasch fundamentals. Without this capacity, enforcement cannot occur consistently.

Finally, evaluation must be iterative. Claims are not accepted permanently. They are monitored, reproduced, refined, or rejected as evidence accumulates.

These steps do not reduce analytical rigor. They restore it.

TRANSITION REQUIRES TRAINING

A transition to meaningful measurement cannot be achieved through policy alone. It requires a parallel investment in training, because representational measurement theory is not intuitive and has never been part of standard professional education in health technology assessment, pharmacoeconomics, or formulary decision making. For more than forty years, practitioners have been taught to work within frameworks that assume measurement rather than demonstrate it. Reversing that inheritance requires structured learning, not informal exposure.

At the center of this transition is the need to understand why measurement must precede arithmetic. Representational measurement theory establishes the criteria under which numbers can legitimately represent empirical attributes. These criteria are not optional. They determine whether addition, multiplication, aggregation, and comparison are meaningful or merely symbolic. Without this foundation, committees are left evaluating numerical outputs without any principled way to distinguish evidence from numerical storytelling.

Training must therefore begin with scale types and their permissible operations. Linear ratio measurement applies to manifest attributes that possess a true zero and invariant units, such as

time, counts, and resource use. Latent attributes, by contrast, cannot be observed directly and cannot be measured through summation or weighting. They require formal construction through a measurement model capable of producing invariant units. This distinction is the conceptual fulcrum of reform, because it determines which claims are admissible and which are not.

For latent trait claims, Rasch measurement provides the only established framework capable of meeting these requirements. Developed in the mid–twentieth century alongside the foundations of modern measurement theory, the Rasch model was explicitly designed to convert subjective observations into linear logit ratio measures. It enforces unidimensionality, tests item invariance, and produces measures that support meaningful comparison across persons, instruments, and time. These properties are not approximations; they are defining conditions of measurement.

Importantly, Rasch assessment is no longer technically burdensome. Dedicated software platforms developed and refined over more than four decades make Rasch analysis accessible, transparent, and auditable. These programs do not merely generate statistics; they explain why items function or fail, how scales behave, and whether a latent attribute has been successfully measured. Measurement becomes demonstrable rather than assumed.

Maimon Research has developed three distance education programs to support the transition to a new paradigm in HTA. These comprise 12 module senior level program that details the standards for measurement, the failure of current HTA standards and the basis for protocol supported claims assessment for ratio measures of manifest attributes and Rasch logic ratio logit measures for latent attributes. The two other programs are only 5 modules but are designed to complement the 12-module program, for measurement axioms and Rasch attribute possession.

Together, these programs equip health systems, committees, and analysts with the competence required to enforce measurement standards consistently. Training does not replace judgment; it enables it. Without such preparation, the transition to meaningful measurement cannot be sustained. With it, formulary decision making can finally rest on claims that are not merely numerical, but measurable.

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DISTANCE EDUCATION PROGRAMS IN THE THEORY OF MEASUREMENT

Three programs are available: two short 5-module programs and a 12-module program that is structured as a senior level course on the transition from the current HTA belief system to a new paradigm for HTA

The two short programs are (i) **NUMERICAL STORYTELLING: SYSTEMATIC MEASUREMENT FAILURE IN HEALTH TECHNOLOGY ASSESSMENT** and (ii) **A NEW START IN MEASUREMENT FOR HEALTH TECHNOLOGY ASSESSMENT**. They are designed to complement the 12-module course program. They can be accessed through the **DISTANCE EDUCATION** section of the website with URL <https://maimonresearch.com/distance-education-programs/>

The senior level course **HEALTH TECHNOLOGY ASSESSMENT REBUILT: EVIDENCE AND VALUE** is accessed through the **EVIDENCE AND VALUE** section of the website or URL link <https://maimonresearch.com/evidence-and-value/>.

DESIGNED FOR CLOSURE

For those who remain unconvinced that there is any need to abandon a long-standing and widely accepted HTA framework, it is necessary to confront a more fundamental question: why was this system developed and promoted globally in the first place?

The most plausible explanation is administrative rather than scientific. Policy makers were searching for an assessment framework that could be applied under conditions of limited empirical data while still producing a determinate conclusion. Reference-case modeling offered precisely this convenience. By constructing a simulation populated with assumptions, surrogate endpoints, preference weights, and extrapolated time horizons, it became possible to generate a numerical result that could be interpreted as decisive. Once an acceptable cost-effectiveness ratio emerged, the assessment could be declared complete and the pricing decision closed. This structure solved a political and administrative problem. It allowed authorities to claim that decisions were evidence-based without requiring the sustained empirical burden demanded by normal science. There was no requirement to formulate provisional claims and subject them to ongoing falsification. There was no obligation to revisit conclusions as new data emerged. Closure could be achieved at launch, rather than knowledge evolving over the product life cycle.

By contrast, a framework grounded in representational measurement would have imposed a very different obligation. Claims would necessarily be provisional. Measurement would precede arithmetic. Each therapy impact claim would require a defined attribute, a valid scale, a protocol, and the possibility of replication or refutation. Evidence would accumulate rather than conclude.

Decisions would remain open to challenge as real-world data emerged. From an administrative standpoint, this was an unreasonable burden. It offered no finality.

The reference-case model avoided this problem entirely. By shifting attention away from whether quantities were measurable and toward whether assumptions were plausible, the framework replaced falsification with acceptability. Debate became internal to the model rather than external to reality. Sensitivity analysis substituted for empirical risk. Arithmetic proceeded without prior demonstration that the objects being manipulated possessed the properties required for arithmetic to be meaningful.

Crucially, this system required no understanding of representational measurement theory. Committees did not need to ask whether utilities were interval or ratio measures, whether latent traits had been measured or merely scored, or whether composite constructs could legitimately be multiplied or aggregated. These questions were never posed because the framework did not require them to be posed. The absence of measurement standards was not an oversight; it was functionally essential.

Once institutionalized, the framework became self-reinforcing. Training programs taught modeling rather than measurement. Guidelines codified practice rather than axioms. Journals reviewed technique rather than admissibility. Over time, arithmetic without measurement became normalized as “good practice,” while challenges grounded in measurement theory were dismissed as theoretical distractions. The result was a global HTA architecture capable of producing numbers, but incapable of producing falsifiable knowledge. Claims could be compared, ranked, and monetized, but not tested in the scientific sense. What evolved was not objective knowledge, but institutional consensus.

This history matters because it explains why the present transition is resisted. Moving to a real measurement framework with single, unidimensional claims does not merely refine existing methods; it dismantles the very mechanism by which closure has been achieved for forty years. It replaces decisiveness with accountability, finality with learning, and numerical plausibility with empirical discipline. Yet that is precisely the transition now required. A system that avoids measurement in order to secure closure cannot support scientific evaluation, cumulative knowledge, or long-term stewardship of healthcare resources. The choice is therefore unavoidable: continue with a framework designed to end debate, or adopt one designed to discover the truth.

Anything else is not assessment at all, but the ritualized manipulation of numbers detached from measurement, falsification, and scientific accountability.

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REFERENCES

¹ Stevens S. On the Theory of Scales of Measurement. *Science*. 1946;103(2684):677-80

² Krantz D, Luce R, Suppes P, Tversky A. Foundations of Measurement Vol 1: Additive and Polynomial Representations. New York: Academic Press, 1971

³ Rasch G, Probabilistic Models for some Intelligence and Attainment Tests. Chicago: University of Chicago Press, 1980 [An edited version of the original 1960 publication]

⁴ Wright B. Solving measurement problems with the Rasch Model. *J Educational Measurement*. 1977;14(2):97-116